Effects of progressive carotid stenosis on cerebral haemodynamics: aortic-cerebral 3D patient-specific simulation

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Effects of progressive carotid stenosis on cerebral haemodynamics: aortic-cerebral 3D patient-specific simulation

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ABSTRACT

We investigated the effects of atherosclerosis in the carotid region on cerebral haemodynamics. A total of 15 stenosis cases following NASCET criteria were modelled using patient-specific medical image data and an open-source package, SimVascular. The formulation adopted the stabilised Petrov–Galerkin scheme with Newtonian and incompressible assumptions. The boundary conditions employed pulsatile inflow and three-element lumped Windkessel outlet conditions with a rigid wall assumption. We present transitions in the represented CoW during stenosis progression using three-dimensional aortic-cerebral vasculature for the first time. This was driven by the conserved total cerebral blood flow to 50% carotid stenosis (CS) (P-value, P > 0.05), which deteriorated during subsequent stages of CS (P < 0.01), and the effective collateral capability of the communicating arteries (CoAs) activated from a degree of 75% and above (P < 0.0001). The prevalence of 'complete' CoW peaked at 50% CS and then declined. Despite the collateral flow, the ipsilateral hemispheric perfusion was moderately reduced (P < 0.01), and the contralateral perfusion was conserved (P > 0.05), revealing the ineffectiveness of collateral capability of CoW at the extreme stages of CS. We identified bulk cerebral auto-regulation effects of the conventional Windkessel model, demonstrating accurate flow reduction in the stenosed artery.

Nomenclature

<table>
<thead>
<tr>
<th>Haemodynamic Properties</th>
<th>tCBF</th>
<th>BFV</th>
<th>Venc</th>
<th>Vavg</th>
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<td></td>
<td>total cerebral blood flow</td>
<td>blood flow volume</td>
<td>encoding velocity</td>
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<th>CoW</th>
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<td>circle of Willis (CoW)</td>
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<td>middle cerebral artery</td>
<td>posterior cerebral artery</td>
<td>communicating artery</td>
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<tr>
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<td>incompletely recruited</td>
<td>completely recruited</td>
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CONTACT Jaiyoung Ryu jairyu@cau.ac.kr

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1. Introduction

The circle of Willis (CoW) is a principal collateral structure that maintains cerebral circulation in response to brain ischaemia, mainly caused by carotid stenosis (CS). The posterior communicating artery (PCoA) and anterior communicating artery (ACoA) serve as collateral links between the anterior and posterior cerebral circulation while reducing the incidence of stroke and transient ischaemic attack (TIA) in both long-term and perioperative follow-up periods (Henderson et al., 2000; Zhou et al., 2016). Incomplete CoW is present in approximately 50–79% of the population (Alpers et al., 1959; Kapoor et al., 2008; Lippert & Pabst, 1985; Papantchev et al., 2013; Riggs & Rupp, 1963) adopting various forms and causing issues such as anterior circulation (Henderson et al., 2000) and lacunar infarctions (Chuang et al., 2008). One important finding is that PCoA hypoplasia is asymptomatic without ipsilateral internal carotid artery (iICA) stenosis (Schomer et al., 1994), but is also a risk factor even without the iICA stenosis (Chuang et al., 2008). This highlights the importance of a more comprehensive study; other confusions also arise: a higher degree of CS is related to the presence of more collaterals (Adams et al., 1999; Hoksbergen et al., 2000; Miyazawa et al., 2011; Morgenstern et al., 1997) but patients with more collaterals had better 90-day (Zhou et al., 2016) and long-term prognoses (Henderson et al., 2000; Kim et al., 2016). The above correlations, however, are reversed in asymptomatic cases as collaterals are less present in such cases than in the symptomatic cases (Hendrikse et al., 2001), with the former experiencing lower benefit from medical intervention (Halliday, 2004; Moneta et al., 1993; Rothwell et al., 1994) implying favorable clinical outcomes even with fewer collaterals. Such contradicting findings may be due to the complexity involved in analyzing the complex anatomy of the individual arterial network in conventional medical approaches and the challenge involved in the patient-specific tracking of CS progression. Alternatively, the correlation between CoW variation and CS is not yet fully understood, as a review (Chatzikonstantinou et al., 2012) suggested that patient-specific follow-up in short time windows is a better clinical approach.

Such complexities have led to various engineering efforts being made, based on both mathematical and experimental techniques. For simplicity, we defined ‘one-dimensional or three-dimensional’ and ‘chin-to-head or aorta-to-head domain’, where the ‘chin-to-head’ and ‘aorta-to-head’ domains were defined as the ICA-to-CoW domain and aortic-cerebral vasculature (ACV), respectively. Although specific cardiovascular conditions such as the occlusion of arteries (Alastruey et al., 2007; Liu et al., 2016; Long et al., 2008; Ryu et al., 2015) and vasospasm (Ryu et al., 2017) have been considered, progressive haemodynamic changes in three-dimensional aortic-cerebral vasculature have not been studied in a patient-specific, large domain (Table 1). Some major limitations of previous studies are as follows: (1) previous studies were unable to describe complex three-dimensional haemodynamic phenomena through one-dimensional analyses (Alastruey et al., 2007; Ryu et al., 2015), (2) a limited coverage of the arterial domain (ICA-to-CoW) was considered in three-dimensional studies (Alnæs et al., 2007; Long et al., 2008; Mukherjee et al., 2018; Zhu et al., 2015a), and (3) the complex physical nature of blood flow was disregarded in CS-correlative clinical or statistical approaches. As suggested in a recent review (Liu et al., 2020), once a large-domain study integrates a three-dimensional simulation and CS, the effects of progressive CS on the flow in the CoW may effectively be captured (Figure 1).

This study was the first to adopt a three-dimensional arterial domain spanning from ACV to simulate various NASCET-based CS conditions. As a result, the effects of progressive CS on cerebral circulation could be analyzed. Our method enabled automatic flow redistribution among the four major arteries (two ICAs, two VAs) and exhibited collateral behavior different from that of the small cerebral domain (Cassot et al., 1995, 2000; Long et al., 2008; Zhu et al., 2015b). Here, the distal collateral flow through ophthalmic and superficial temporal arteries was discounted as such re-routing of blood flow may occur only during severe bilateral CS (Yamamoto et al., 2004); only unilateral CS was employed in this study. While progressive unilateral CS causes abnormal flow distribution in vasculatures (Cassot et al., 1995, 2000; Henderson et al., 2000; Moneta et al., 1993; Mukherjee et al., 2018; Rothwell et al., 1994; Schomer et al., 1994), the present study focused on variant forms of CoW and the role of CoAs in cerebral circulation.

2. Methods

2.1. Patient-specific, three-dimensional haemodynamics

Patient-specific CTA data were obtained with the approval of the Institutional Review Board (IRB) from a medical-image database from Screening Technology and Outcome Project (STOP) in a stroke database study (Smith et al., 2009). The selected images covered most of the upper-chest arterial domain ranging from the aorta to the CoW. Four models, identical to Mukherjee...
et al. (2016), were chosen, but one, pat2, was excluded due to its string-like ICAs since they may already exhibit occlusive behavior. All models displayed anatomical features of (1) a complete CoW and (2) distinctive branching patterns of arterial vessels downstream of the aortic arch. This variety in haemodynamic structure showed different flow distribution types (Mukherjee et al., 2016), ensuring the reliability of the present study (Figure 1A).

### 2.2. Model geometry

CTA images had mean voxel size of $511 \times 511 \times 439.7$ (±31.8, SD) and a resolution of $0.46 \times 0.46 \times 1$ mm. The CTA-based computational domains were then constructed using an open-source haemodynamics simulation package, SimVascular (Updegrove et al., 2017), and all patient models underwent the two-dimensional vessel segmentation.
procedure (Wilson et al., 2001). The centerline paths in each image were combined with segmented two-dimensional contours, which were automatically lofted to create wall boundaries for the arterial domain. The meshing process finalized the solid computer model with a three-dimensional, tetrahedral grid structure.

2.3. Numerical scheme

Although blood is a non-Newtonian fluid in which viscosity depends on the hematocrit (Berger & Jou, 2000; Pedley & Luo, 1995), it can be assumed as a Newtonian fluid when large arteries, such as the cerebral artery, are simulated (Arzani, 2018; Ku, 1997; Taylor & Figueroa, 2009). Hence, blood in the arterial system was assumed as a Newtonian fluid with a density of 1.06 g cm$^{-3}$ (Trudnowski & Rico, 1974) and viscosity of 0.04 g s$^{-1}$ cm$^{-1}$ (Hall & Hall, 2020). With rigid wall assumptions, a Petrov–Galerkin stabilized finite-element formulation with linear elements (Brooks & Hughes, 1982; Franca et al., 1992; Franca & Frey, 1992) was used to calculate the flow velocity and pressure field of the constructed domains. The Navier-Stokes equations with the above assumptions and the corresponding Petrov-Galerkin formulation can be expressed as,

$$
\rho_f \left( \frac{\partial u}{\partial t} + (u \cdot \nabla) u \right) = -\nabla p + \nabla \cdot \tau + \rho_f g \tag{1}
$$

$$
\nabla \cdot u = 0 \tag{2}
$$

$$
\tau = 2\mu_f D(u) = \mu_f (\nabla u + \nabla u^T) \tag{3}
$$

$$
\rho_f \left( \frac{\partial w}{\partial t} \right)_{\Omega} + \rho_f (w, (u \cdot \nabla) u)_{\Omega} + 2\mu_f (D(w), D(u))_{\Omega} - \rho_f (w, b)_{\Omega} = - (\nabla \cdot \rho)_{\Omega} - (\nabla \cdot q)_{\Omega} + (q, u \cdot n)_{\Gamma} - \left( \frac{(w, b)_{\Gamma, \Omega_{\Gamma}}}{} \right)_{\Phi_{\Gamma}} + \left( \frac{(w, h_{\partial})_{\Gamma, \Omega_{\Gamma}}}{} \right)_{\Phi_{\Gamma}} + \frac{\sum_{\varepsilon=1}^{N_d}}{} \left( \tau_{\text{pspg}} \frac{\nabla h}{\nabla \cdot \tau_{\text{pspg}}} \frac{\nabla h}{\nabla \cdot \tau_{\text{pspg}}} \frac{\nabla h}{\nabla \cdot \tau_{\text{pspg}}} \frac{\nabla h}{\nabla \cdot \tau_{\text{pspg}}} \right)_{\Phi_{\Gamma}} \tag{4}
$$

where Eqs. (1), (2), (3), and (4) are the Navier-Stokes equation, continuity equation, constitutive law for Newtonian fluids, and a general variational form of the stabilized finite-element method, respectively. Here, $u$ and $p$ are the velocity and pressure fields, $w$ and $q$ are the corresponding test functions, $\rho_f$ is the density of blood, $\mu_f$ is the viscosity of blood, $g$ is gravitational acceleration, $b$ denotes the total body force, $h$ denotes the contributions at each Neumann boundary ($\Gamma$) of the computational domain ($\Omega$), $D$ denotes the symmetric part of the velocity gradient ($\nabla u + \nabla u^T$), and $R^h$ is the corresponding element residual of the momentum equation. The stabilization parameters $\tau_{\text{pspg}}$ and $\tau_{\text{pspg}}$ are chosen as functions of the element size (Franca & Frey, 1992; Tezduyar & Osawa, 2000). The term $h_{\partial}$ is the contribution to the variational form from all the resistance outflow boundary conditions (Vignon-Clementel et al., 2006, 2010). The finite-element solver, with customized preconditioners, was implemented as a part of the SimVascular package (Updegrove et al., 2017), which has been validated for accurately adapting patient-specific boundary conditions (Coogan et al., 2013; Mukherjee et al., 2018; Vignon-Clementel et al., 2006) and describing flows in larger arteries (Les et al., 2010; Mukherjee et al., 2016). Details about the solver are available in Esmaily-Moghadam et al. (2013).

2.4. Boundary conditions

The prescribed inlet condition was a pulsatile flow rate of ascending aorta in Olufsen et al. (2000), assigned to all patient geometries. Since the inlet velocity profile of ascending aorta is generally plug-type (Seed & Wood, 1971), such type was mapped on to the face of the aorta inlet. The outlet boundary conditions were given at distal ends of each branch as three-element lumped parameter Windkessel models, providing two resistances of proximal resistance $R_p$ and distal resistance $R_d$ and one capacitance $C$. Total resistance $R_t (R_t = R_p + R_d)$ was calculated with MAP, and total cardiac volumetric flow $Q$ acquired from inlet flow using the relation $\text{MAP} = Q \cdot R_t$. The ratio $\alpha$ was given as $\alpha = R_p/(R_p + R_d)$ and a fixed value of 0.91 was selected for a total of eleven Windkessel outlets. Total capacitance $C_{\text{tot}}$ was initially calculated using the relation $C_{\text{tot}} = dV/dP$ and distributed to outlets depending on their cross-sectional area to provide individual values of $C$ at each outlet. All values of $C$ then were iteratively optimized until feasible pressure ranges were achieved using a conventional procedure (Xiao et al., 2014). MAP was calculated as $(P_{\text{sys}} + 2P_{\text{dia}})/3$ with $P_{\text{sys}}$, and $P_{\text{dia}}$ as systolic and diastolic pressures, and flow distribution was set to be equivalent to Mukherjee et al. (2016). Iterative tuning of individual resistance values was conducted to obtain desired outflow rates during steady-state simulation, and capacitance values were tuned to match acceptable pulse pressure range of 40–50 mmHg for the descending aorta and its nearest region and 30–40 mmHg for carotid and cerebral arteries (Alastruey et al., 2007; Coogan et al.,...
Specific boundary conditions for each patient model. Pulsatile inflow (reproduced from Olufsen et al., 2000) was given at the aorta, and Windkessel 3-element outlet conditions were used for a total of eleven outlet boundaries.

Table 2. Windkessel RCR parameters of all patient models. $R_p$, $R_d$, and $C$ represent proximal resistance, distal resistance, and compliance, respectively. The units for resistance and compliance are $10^9$ Pa/s/m$^3$, and $10^{-10}$ m$^3$/Pa, respectively.

<table>
<thead>
<tr>
<th>Artery</th>
<th>$R_p$</th>
<th>$C$</th>
<th>$R_d$</th>
<th>$R_p$</th>
<th>$C$</th>
<th>$R_d$</th>
<th>$R_p$</th>
<th>$C$</th>
<th>$R_d$</th>
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<tr>
<td>DsA</td>
<td>0.02</td>
<td>225.4</td>
<td>0.18</td>
<td>0.02</td>
<td>221.2</td>
<td>0.19</td>
<td>0.02</td>
<td>280.1</td>
<td>0.19</td>
</tr>
<tr>
<td>cACA</td>
<td>0.91</td>
<td>0.9</td>
<td>9.24</td>
<td>0.71</td>
<td>1.2</td>
<td>7.21</td>
<td>0.73</td>
<td>0.5</td>
<td>7.43</td>
</tr>
<tr>
<td>cECA</td>
<td>0.44</td>
<td>2.3</td>
<td>4.42</td>
<td>0.40</td>
<td>2.5</td>
<td>4.00</td>
<td>0.28</td>
<td>2.3</td>
<td>2.80</td>
</tr>
<tr>
<td>cMCA</td>
<td>0.53</td>
<td>0.9</td>
<td>5.04</td>
<td>0.57</td>
<td>0.9</td>
<td>5.78</td>
<td>0.56</td>
<td>0.8</td>
<td>5.62</td>
</tr>
<tr>
<td>cPCA</td>
<td>0.78</td>
<td>0.8</td>
<td>7.85</td>
<td>1.10</td>
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<td>11.14</td>
<td>0.82</td>
<td>0.5</td>
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<td>0.14</td>
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<tr>
<td>iACA</td>
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<td>0.8</td>
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<td>0.4</td>
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<tr>
<td>iECA</td>
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<td>0.73</td>
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<td>0.4</td>
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<tr>
<td>iSA</td>
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<td>1.34</td>
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<td>10.9</td>
<td>1.41</td>
<td>0.16</td>
<td>16.7</td>
<td>1.59</td>
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A graphical illustration of the boundary condition is shown in Figure 2 and the patient-specific three-element Windkessel boundary conditions are given in Table 2.

The resistance conditions in the distal regions of the arterial outlets were assumed not to change despite the progression of CS. It mainly was due to the innate nature of the arterial networks, which are closed-loop systems. Cardiac perfusion might also have been affected due to severe CS causing acute cardiac compensation, as in a coarctation case (Coogan et al., 2013), but since the cerebral flow was only 14% of the total cardiac output (Kety, 1950), its impact was assumed negligible.

2.5. Data analysis

An open-source program ParaView (Kitware, Inc. Clifton Park, NY, USA) (Schroeder et al., 2004) was used to analyse and post-process the simulation results.

The definitions of the blood flow volume (BFV) and normalized flow rates were calculated with equations given below.

\[
BFV = \int_{t=0}^{t_p} Q_{\text{mean}} dt \quad (5)
\]

\[
\text{Normalized Flow Properties} = \frac{Q_i}{Q_n} \quad (6)
\]

where $t_p$, $Q_i$, and $Q_n$ represented the period of the cardiac cycle, the flow rate at the corresponding severity in CS, and the flow rate at the absence of CS (0%), respectively.

The total flow across the CoAs (tCoA) was proposed in this study. This was expressed as the sum of the absolute flow rate across the CoAs representing the movement of the collateral flow within a CoW. The equation is given below as,

\[
t_{\text{CoA}} = |BFV_{ACoA}| + |BFV_{iPCoA}| + |BFV_{cPCoA}| \quad (7)
\]

where $BFV_{ACoA}$, $BFV_{iPCoA}$, and $BFV_{cPCoA}$ were the corresponding BFV of the given arteries. For simplicity, the flow directions for the CoAs were defined similarly to previous studies (Alastruey et al., 2007; Ryu et al., 2017); the PCoA direction was positive towards anterior circulation and the ACoA direction was positive to the ipsilateral side (Figure 3).

Moreover, a peak systolic velocity (PSV) threshold, considered to be similar to the fading limits of encoding velocity ($V_{\text{enc}}$) in the present study, was selected for the iso-volumetric representation of CoW. $V_{\text{enc}}$ can even go up to 40 cm/s for the detection of PCoAs (Schomer et al., 1994), but the threshold range of the average velocity was determined to be 3–15 cm/s based on the recent small cerebral artery literature (Schnerr et al., 2017).

2.6. NASCET criteria and ECST conversion

NASCET criteria (Moneta et al., 1993) is calculated with the equation below,

\[
\text{NASCET} = 1 - \frac{D_i}{D_n} \times 100(\%) \quad (8)
\]
where $D_n$ and $D_s$ represent the distal diameter of the stenosed artery observed to be normal and the narrowest diameter at the stenosis, respectively. The severities selected to simulate the progressive effects of CS were 0, 50, 75, 85, and 95%. The criteria had to be converted to ECST (Rothwell et al., 1994) for accurate comparison with the literature that did not employ NASCET criteria. The conversion equation (Rothwell et al., 1994) is presented below,

$$ECST(\%) = 0.6 \cdot NASCET(\%) + 40\% \quad (9)$$

This made the corresponding ECST-based severities to our study 40, 70, 85, 91, and 97%. However, a 0% NASCET denotes the absence of stenosis, and thus, the ECST severities were rearranged as 0, 70, 85, 91, and 97%. The stenosis was given on the proximal segment of the right internal carotid artery (RICA) near the carotid bifurcation (Figure 4A). The lumen diameter of the target location hence changed to the corresponding severity, and the fixed origin of the stenosis, located at the centerline, enabled the stenosis to be symmetric.

### 2.7. Grid independence test

The computational mesh containing $6\times8.5 \times 10^6$ elements was similar in number to those from Mukherjee et al. (2016) and Mukherjee et al. (2018), which was already verified using a more detailed mesh-refinement study (Les et al., 2010) and coarctation study (Coogan et al., 2013). However, since the present study imposed stenosis conditions to iICA, the local mesh around iICA had to be validated. Validation made using an iICA-only domain is unidentical to the result using the whole domain, and hence the test was carried out using the whole domain. The haemodynamic properties of PSV and systolic pressure $P_{sys}$ were chosen for validation to represent the extreme conditions at the stenosis region. As a result, case 2 was chosen for 95% CS case of P01, and mesh sizes were evenly scaled to their corresponding stenosis diameter for all patient cases (Table 3). The same process was applied to the rest of the CS severity.

### 2.8. Statistics

The differences in moderate and severe stenosis results were statistically evaluated by Student’s $t$-test or Welch’s $t$-test depending on the results of Levene’s test. No results were excluded. Statistical test results were designated with n.s. (no significance) when $P > 0.05$, one asterisk (*) when $P < 0.05$, two asterisks (**) when $P < 0.01$, three asterisks (***) when $P < 0.001$, and four asterisks (****) when $P < 0.0001$.

### 3. Results

#### 3.1. Progressive changes in BFV of iICA and tCBF reduction

The following results include data for all three patient models. The progressive changes in the aortic-cerebral haemodynamics of P02 during the subsequent progression of CS (P01 and P03 are available in Supplemental Figures II to IV) were observed in Figure 4A. Figure 4B shows the normalized MFR in the four major arteries leading to the CoW in ECST standard. The values were normalized from a baseline, 0% stenosis. As stenosis progressed, the BFV ratio in iICA fell rapidly after 70% severity, falling within the range of the theoretical single-pipe (Spencer & Reid, 1979) and in-situ measurement value (Berguer & Hwang, 1974). The result from Long et al. (2008), however, diverged from the literature at severe stenoses. Based on this result, the groups of moderate (< 70%), and severe (> 70%) were created which a total of six, and nine cases were allocated for moderate, and severe, respectively. Figure 4C compares the BFV in major arteries leading to CoW (iICA, cICA, iVA, and cVA) grouped in moderate (< 70%), and severe (> 70%). The changes in ICAs were very significant ($P < 0.0001$), VAs experience relatively minor changes ($P < 0.01$). Figure 4D shows the resultant changes in flow distribution in both hemispheres. The ipsilateral
Figure 4. A, 3D PSV contour of P02 showing the continuous changes of cardiovascular haemodynamics during the progression of CS. The trend was identical in all patient models. B, Comparison of flow rate ratio (FRR) with the literature. The flow rate under stenosis, $Q_s$, and under normal (0%) condition, $Q_n$, were used for clear comparison of the tendencies. Present results were depicted in a group of red dots with mean and standard deviation in black lines. C, Blood Flow Volume (BFV) in major arteries (iICA, cICA, iVA, and cVA) leading to CoW in the moderate (< 70%) and severe (> 70%) groups. D, The flow distribution to the ipsilateral and contralateral hemisphere in the moderate and severe groups. E, BFV in communicating arteries (cPCoA, iPCoA, and ACoA) in the moderate and severe groups. F, BFV of total cerebral blood flow (tCBF) and total flow across CoAs (tCoA) in the moderate and severe groups. Notations were given for $P$ values of: $>0.05$; n.s., $<0.05$; *, $<0.01$; **, $<0.001$; ***, $<0.0001$; ****.

Table 3. Grid independence test of P01 at 95% CS.

<table>
<thead>
<tr>
<th>Cases</th>
<th>No. of elements $(10^6)$</th>
<th>PSV (cm/s)</th>
<th>$\Delta$ (%)</th>
<th>$P_{sys}$ (mmHg)</th>
<th>$\Delta$ (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Case 1</td>
<td>7.84</td>
<td>428.61</td>
<td>–</td>
<td>127.00</td>
<td>–</td>
</tr>
<tr>
<td>Case 2</td>
<td>8.47</td>
<td>432.98</td>
<td>1.02</td>
<td>127.72</td>
<td>0.57</td>
</tr>
<tr>
<td>Case 3</td>
<td>9.66</td>
<td>436.18</td>
<td>0.74</td>
<td>128.13</td>
<td>0.32</td>
</tr>
</tbody>
</table>

PSV, peak systolic velocity; $P_{sys}$, systolic pressure; $\Delta$, percent change between the previous and the present value.

Side was affected significantly ($P < 0.01$) while the effects on the contralateral hemisphere were minimal (n.s.). Figure 4E shows BFV in CoAs. From moderate to severe, the changes in cPCoA were negligible (n.s.) while both iPCoA and ACoA were affected severely ($P < 0.0001$). In quantity, ACoA was affected the most. Figure 4F shows the tCBF and tCoA in BFV of two groups, moderate and
severe. The progression of CS made significant changes in both tCBF ($p < 0.01$) and tCoA ($p < 0.0001$). Overall, tCBF was reduced at severe CS, which provoked the increased flow rate across CoAs, the collateral arteries. A similar but less dramatic tendency in the CoAs was observed by Cassot et al. (1995).

### 3.2. Bulk auto-regulation effect in ACV

Figure 5A-1 shows a comparison of the tCBF ratio in the present study and those of Zhu et al. (2015b) and Long et al. (2008), which did not use a cerebral auto-regulation model (CAM). The tCBF in the present study was maintained until 50% CS but gradually fell until 95% CS, significantly different from those of Zhu et al. (2015b) and Long et al. (2008). Figure 5A-2 shows a comparison of the tCBF ratio in the present study and the literature with CAM. The results match well with the study employing CAM (Cassot et al., 1995). Figure 5B-1 shows a comparison of the BFV ratio in MCA, ACA, and PCA in both hemispheres. The arteries were grouped based on the changes in BFV ratio, and three groups were made (first group, all contralateral arteries and iPCA; second group, iACA; and third group, iMCA). A comparison in the first group showed negligible differences. Both the flow in iMCA and iACA from the present study, however, showed similar trends in their BFV ratio along with CS progression while the results from Zhu et al. (2015b) drastically changed even at 50% CS. Figure 5B-2 shows a comparison of BFV in CoAs with the ones from Cassot et al.
Figure 6. A, Velocity streamlines around PCoAs at their systolic phases of P01. The tendencies were identical in all patient models. The locations of the PCoAs (arrows; dark blue) are indicated. Note the drastic increase in flow velocity in the iPCoAs during the progressive CS and consistent flow velocity in cPCoAs. CS progression also provoked the recirculation in the ipsilateral region and rapid flow in the collateral arteries. The percentages note the severity of the stenosis; B, Flow rates in the CoAs. Flow rates in ACoA and iPCoA experienced dramatic changes moving to the positive direction showing minor jumps at 50% stenosis, and major leaps from 75% CS, triggering the flow of notable amount of blood volume. Their waveforms from 75% CS resembled the ones of normal arteries. The flow rates in cPCoA, however, remained relatively unchanged.

3.3. CoA response to ICA stenosis

Figure 6A shows the velocity streamlines around PCoAs of P01. This was identical in the results of other patient models (P02 and P03 are available in Supplemental Figure V). The drastic increase in the flow of iPCoA was visually emphasized with red color and streamlined with a velocity above 100 cm/s, while the one in cPCoA remained unchanged. The streamline in iPCoA remained still until 50% CS, but a transition occurred from 75% CS. The severe CS also affected the arteries around PCoAs: the flow in iICA became highly circulatory, and the one in BA significantly increased, while the one in cICA was also considerably increased. Figure 6B shows the flow rate waveforms in CoAs, namely ACoA, iPCoA, and cPCoA. At severities below 50%, the waveform oscillated around zero-value. The progression of CS until 50% had a negligible impact on the waveform of all CoAs. Further progression to 75% dramatically impacted the waveforms of ACoA and iPCoA but negligibly impacted cPCoA. The waveforms of ACoA and iPCoA at a severity above 75% resembled the ones of normal arteries.

3.4. Variation in CoW during CS progression

Figure 7A shows three-dimensional velocity magnitude contours of the CoW and representative iso-volumetric surfaces in P02. The changes in the velocity contours were identical to the velocity streamline in Figure 7A, and due to similarities in its tendency, only the P02 case was presented (P01 and P03 are available in Supplemental Figure VI). The surfaces are graphical depictions of the superior view of the CoW contours, with values of PSV greater than 12 cm/s. The PSV value was determined using the concept of $V_{\text{enc}}$ in conventional maximum intensity projection (MPI) technique using MRI. For MPI in magnetic resonance angiography (MRA), $V_{\text{enc}}$ is set to project the vessel network. $V_{\text{enc}}$ is set slightly higher than the maximum expected velocity due to aliasing of data, where both the magnitude and the direction of the flow are significantly reduced and reversed at a flow velocity greater than $V_{\text{enc}}$. The key issue here is that, when this value is set too high, small arteries and near-wall arterial boundaries with low-velocity magnitudes may be considered as noise and hence be eliminated. In this study, velocity
thresholds were imposed in the range of 3–15 cm/s in average velocity ($V_{avg}$), based on Schnerr et al. (2017), and twice for PSV, 6–30 cm/s, assuming Poiseuille flow. The iso-volumetric surfaces of all patient models are available in Supplemental Figures II to XII.

This approach resulted in two distinct phenomena in the iso-volumetric surface: incompletely recruited (IR) and completely recruited (CR) arterial segments. This was a result of adopting the rigid body assumption in the complete CoW domain, where arteries could be incompletely filled depending on the threshold. The typical cases of IR and CR are illustrated in Figure 7B, where IR parts are indicated with purple arrows. The arterial segments with minimum diameters less than half of the rigid body arteries were IR. The velocity thresholds were imposed with equivalent intervals for each velocity type, creating a total of one hundred and fifty iso-volumetric surfaces. Figure 7C was plotted based on the data from the one hundred and fifty surfaces, and CR was seen dominantly in 50% CS. The prevalence of CR in 0, 75, and 85% CS was almost half of that in 50% CS. CR was not seen in 95% CS. While there was a tendency in the prevalence of CR, it vanished in the comparison between two groups of moderate and severe (n.s.).

### 3.5. Validation

The present results were also compared to other haemodynamic studies (Coogan et al., 2013; Olufs et al., 2000; Pagoulou et al., 2017) and clinical measurements of US (Nicolau et al., 2001) and MRA (Oktar et al., 2006) data.

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**Figure 7.** A, 3D velocity contours and the representative iso-volumetric 3D surfaces at the peak systole. The peak systole here represented the maximum velocity magnitude in individual voxels in a cardiac cycle which is a similar representation as MIP in the medical imaging techniques such as transcranial Doppler (TCD) or MRA. The arrows indicated reversed flow from the contralateral side to the iMCA (red; blank), and unrecruited/incompletely recruited arteries (purple; filled); B, the difference between the IR and CR part of the artery segment indicated with and arrow (purple) is shown. The prevalence of CR-CoW during CS progression are presented in C, The prevalence of CR-CoW at each stages of CS. In moderate ( < 70%) and severe ( > 70%) groups, there was no difference (n.s.). This implied that IR-CoW can be present depending on the imaging threshold, and CR-CoW be a potential transitional stage between various forms of IR-CoW.
Both MAP and BFV fell within narrow error ranges, and the BFVs of VA, especially, had almost equivalent mean value and even a smaller SD. The BFV in the stenosed ICA was unavailable but a corresponding comparison is shown in Figure 4A-1.

4. Discussion

4.1. tCBF consistency during CS progression

In this study, for the first time, an ACV was employed for a predictive study of CS. The RICA was selected for each patient model to apply the NASCET-based stenosis conditions, and a total of fifteen cases were created. Previous studies assumed new inflow conditions at the ICAs, VAs, or BA to the corresponding stenosis conditions due to unknown boundary conditions during severe stenosis, but such an approach was unnecessary in our extended domain. In our domain, these unknowns were calculated directly using the Navier-Stokes equations with validated assumptions. The blood flow in iICA was calculated using the change in the local resistance, proportional to the local cross-sectional area, and the reduced flow rate in iICA was automatically redistributed to the other arteries such as the DsA, SA, and ECA (Table 5). The reduced flow rate in iICA to the cerebral region was redirected via cICA, iVA, and cVA (Figure 4C), in which increments were significant (P < 0.01) in all three arteries. Such redirection of flow resulted in a considerable reduction in flow distribution (P < 0.01) to the ipsilateral hemisphere (Figure 4D, Table 5). The flow in iICA from the present study showed equivalent values to those presented in Spencer and Reid (1979) and Berguer and Hwang (1974), which were validated with ultrasonography (US) data. The iICA flow rate from Long et al. (2008), which used a somewhat shorter domain comprising only distal ICA and CoW (ICA-to-CoW domain), which were approximately one-seventh times shorter longitudinally than the large arterial domain (typically spanning from the aorta to the cerebral vasculature). They did not employ a CAM as in the present study, but their results were different from our results showing that tCBF was maintained to 50%, while gradual decrements were shown at subsequent stages of CS progression. The flow reduction in the present study was also minimal compared to both Zhu et al. (2015b) and Zhu et al. (2015a). Hence, the difference in the tCBF ratio should be due to the use of ACV in the present study. Moreover, our tCBF result without the auto-regulation model mirrors the auto-regulated results from Cassot et al. (1995). This result suggests that a considerably large arterial domain, such as ACV, covering both long proximal and distal segments from the region of interest, has bulk autoregulatory effects similar to vascular models with auto-regulation effects. It was one of the major differences seen in the ACV model in comparison to using the conventional small arterial domain. Another difference was that even though the tCBF results were identical to the ones using the auto-regulation model (Cassot et al., 1995), the BFVs in CoAs were significantly different (Figure 5A-2, 5B-2). The individual BFV in ACV and iPCoA in the present study followed a similar trend to the tCBF result; it maintained BFV until 50% with increments during the subsequent CS. The results of Cassot et al. (1995) showed a rather gradual increment from 0% CS, which difference speculated to be due to the use of the ICA-to-CoW domain in the reference. This suggests that the use of an ACV is an appropriate approach for the effective modeling of arterial domains to investigate the effects of progressive CS on CoW haemodynamics.
Table 4. Comparison of the averaged MAP and BFV with values from the literature.

<table>
<thead>
<tr>
<th>Study</th>
<th>DsA</th>
<th>iSA</th>
<th>iMCA</th>
<th>iACA</th>
<th>Remark</th>
</tr>
</thead>
<tbody>
<tr>
<td>Present</td>
<td>95.2</td>
<td>94.1</td>
<td>87.1</td>
<td>85.4</td>
<td>3-D</td>
</tr>
<tr>
<td>Coogan et al. (2013)</td>
<td>102.0</td>
<td>–</td>
<td>89.0</td>
<td>–</td>
<td>3-D</td>
</tr>
<tr>
<td>Pagoulatou et al. (2017)</td>
<td>91.9+</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>Experimental</td>
</tr>
<tr>
<td>Olufsen et al. (2000)</td>
<td>98.3</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>1-D</td>
</tr>
</tbody>
</table>

Table 5. Average flow distribution of arteries and hemispheric flow distribution with CS progression.

<table>
<thead>
<tr>
<th>Artery</th>
<th>Average flow distribution (% ± SD) in arteries</th>
<th>Average flow distribution (% ± SD) in hemispheres</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Artery</td>
<td>0</td>
</tr>
<tr>
<td>DsA</td>
<td></td>
<td>67.17 ± 0.68</td>
</tr>
<tr>
<td>iSA</td>
<td></td>
<td>8.76 ± 0.60</td>
</tr>
<tr>
<td>eECA</td>
<td></td>
<td>3.53 ± 0.82</td>
</tr>
<tr>
<td>iMCA</td>
<td></td>
<td>2.28 ± 0.48</td>
</tr>
<tr>
<td>iACA</td>
<td></td>
<td>1.32 ± 0.12</td>
</tr>
<tr>
<td>iPACA</td>
<td></td>
<td>1.11 ± 0.13</td>
</tr>
<tr>
<td>cSA</td>
<td></td>
<td>7.61 ± 0.99</td>
</tr>
<tr>
<td>cECA</td>
<td></td>
<td>3.41 ± 0.65</td>
</tr>
<tr>
<td>cmCA</td>
<td></td>
<td>2.11 ± 0.05</td>
</tr>
<tr>
<td>cACA</td>
<td></td>
<td>1.51 ± 0.17</td>
</tr>
<tr>
<td>cPCA</td>
<td></td>
<td>1.22 ± 0.20</td>
</tr>
</tbody>
</table>

while minor differences from the autoregulatory model were observed in the CoAs.

4.3. Role of CoAs during CS progression

CoAs are known to play significant roles in providing collateral flow during occlusive arterial conditions (Alastruey et al., 2007; Cassot et al., 1995, 2000; Chuang et al., 2008; Henderson et al., 2000; Hoksbergen et al., 2003; Mukherjee et al., 2018; Ryu et al., 2015; Zhu et al., 2015b), and other cerebral diseases (Adams et al., 1999; Kim et al., 2016; Schomer et al., 1994; Zhou et al., 2016). They provide excessive blood flow in the collateral arteries (iVA, cVA, and cICA) to the ipsilateral hemisphere but, as a consequence, are dramatically affected during the occlusion of the ICAs and VAs (Alastruey et al., 2007; Cassot et al., 1995, 2000; Morgenstern et al., 1997; Mukherjee et al., 2018). Their roles during the progressive CS have also been studied, and they have shown either gradual increases (Zhu et al., 2015b) or drastic changes depending on their diameter (Alastruey et al., 2007; Cassot et al., 1995, 2000). However, in our larger,
three-dimensional arterial domain, the results were quite different; the changes in the MFR of the CoAs were negligible until 50% but dramatically altered during severe stenosis (Figure 4E, 4F). This redirection of flow via collateral arteries maintained the tCBF well (Figure 4F), while the major contralateral cerebral arteries remained unaffected (Figure 4E). Overall, the progressive CS provoked immediate responses of both the iPCoA and ACoA. Consequently, the loss of ipsilateral hemispheric perfusion was compensated, but the responses were more dramatic compared to those reported in the literature.

4.4. Effects of progressive CS on CoAs

The impact of progressive CS on the CoAs haemodynamics was significant. Specifically, ACoA and iPCoA were severely affected, while its effects on cPCoA were negligible (Figure 6A, 6B). The latter was due to the increase in BFV of both cICA and cVA (Figure 4C), which resulted in negligible changes in the flow distribution to the contralateral hemisphere (Figure 4D). In the cases of P2 and P3, CS altered the flow direction in ACoA and PCoA towards the positive direction. The effects of CS especially were seen in Figure 6A, where high-velocity flows were observed only in iPCoA with a severity above 75%. During the progression, the flow in cPCoA fluctuated, but the changes were insignificant (Figure 6B).

Interestingly, BFVs in both ACoA and iPCoA were almost zero until 50% CS (Figure 4F, 5B-2), although the flow fluctuated with considerable amplitudes. The shapes of the waveforms in ACoA and iPCoA at CS greater than 75% resembled the waveforms of normal arteries, implying active involvement of ACoA and iPCoA in cerebral circulation during the severe unilateral CS. These results followed the statistical correlations described in Schomer et al. (1994) and Wang et al. (2016), further validating the BFVs of our study. The transition in BFV of major arteries during low-to-moderate CS is thus another novel contribution of our study. The minimal changes in the waveform of cPCoA indicate that the effect of severe unilateral CS on the contralateral hemisphere was insignificant (Figure 5B-2, 6B), implying the involvement of cPCoA was trivial during severe unilateral CS.

The diversity of the initial-stage flow waveforms in CoAs may be due to the innate asymmetry of the upper-chest arterial network (Figure 1C). The perfect balance between the hemispheric circulations may not always be achieved, even under normal conditions (Table 5). The presence of blood flow, even without CS suggests that CoAs may exist due to the unequal distribution of cerebral flow through the main arteries. These arteries with significantly reduced flow rates may either be undetected or excluded from MRA analysis, mainly due to being considered as noise factors, as suggested in Hoksbergen et al. (2003), Cassot et al. (1995), and Alastruey et al. (2007). Overall, ACoA may provide cross-collateral flow due to the difference in haemodynamic demands between the ipsilateral and contralateral sides and the PCoAs for the differences in anterior and posterior circulation on their corresponding sides.

4.5. Transitional stages of CoW during CS progression

For the first time, our results showed stepwise variations of the CoW configurations in response to unilateral ICA stenosis with three-dimensional velocity magnitude and iso-volumetric contours (Figure 7A). While the velocity contours intuitively show the abrupt changes in the velocities of the ipsilateral cerebral arteries, the iso-volumetric contours illustrated the representative changes in the visibility of the arteries. The correlation of the absent functionality of A1 to severe CS has been demonstrated by Hoksbergen et al. (2003), but our results showed that A1 became functional again with the redirected flow from the contralateral hemisphere at 95% severity, which is coherent with the findings made using US data (Saqqur et al., 2018). The PCoAs also became functional at the ipsilateral side in response to ipsilateral CS progression while the contralateral side remained inactive (Figure 7A).

These phenomena caused IR and CR conditions in our representative iso-volumetric contours, as described in Section 3.4 and Figure 7B, respectively. When thresholds were imposed on CoW, the CoW with CR conditions was observed the most in 50% CS and evenly observed in 0, 75, and 85% CS (Figure 7C). The CR-CoW was not present at the near-occlusion state (95%), and the overall trend demonstrated a general pulsatile cardiac waveform. CR-CoW was most present in 50% CS, but when the groups were re-classified into moderate (< 70%) and severe (> 70%), the statistical correlation between the two groups was not significant (n.s.). This implies that, even though the progression of CS created a distinct variation pattern in the CoW, a holistic analysis of CoW variation might provide statistically insignificant information. Such inclination became more dominant in PSV-based classification (Supplemental Figure XIII). The authors thought such disagreement in the cerebral haemodynamics during the progression may have led to the conflicting arguments in Hoksbergen et al. (2003) and Chuang et al. (2008), and even slightly confusing arguments in Banga et al. (2018), which correlated the isolated iMCA (of various forms) to a neurological disease while
neglecting the high prevalence of both severe ipsilateral and contralateral CS.

The above discussion highlights that the complete CoW may not always be a golden standard for better clinical outcomes. The initial fluctuating waveform in CoAs until 50% stenosis (Figure 6B) made the posterior circulation IR in the represented CoW (Figure 7A). The CoW was CR at 50 and 75% but IR at 85% and 95%, although ACoA and iPCoA at 75% and above showed waveforms (Figure 6B) resembling those of normal arteries (Figure 2, inlet waveform). Patient-wise, CoW was CR at 50 and 75% but IR at 85% and 95%, although ACoA and iPCoA at 75% and above showed waveforms (Figure 6B) resembling those of normal arteries. The CoW was CR at 50 and 75% but IR at 85% and 95%, although ACoA and iPCoA at 75% and above showed waveforms (Figure 6B) resembling those of normal arteries.

This may also be related to the collateral capacity of the cerebral circulation. The tCoA increased with stenosis progression to maintain cerebral circulation, but only until 50% stenosis (Figure V). After that, the tCBF gradually reduced by the resultant difference between the tCoA, and the flow in iICA. This meant that the major carotid and cerebral arteries had their collateral capacities maintained until 50% stenosis, which later led to the gradual depletion of the collateral reserve during the further progression of CS. Overall, the collateral capacity switched with the active involvement of both iACA and iPCoA caused variations in the CoW during unilateral CS (Supplemental Figure V). Therefore, the classifications of the CoW may have to be contemplated for more accurate statistical comparisons.

4.6. Limitations

This study had several limitations. First, one of our assumptions was a rigid vessel wall. Arterial compliance is typically regulated with diameters of deformable vessel walls, and the diameters are affected by the pulsatile nature of the blood flow. Once a fluid-structure interaction (FSI) model is employed, such large displacements and deformations of the arterial wall also need to be solved numerically. An arbitrary Lagrangian–Eulerian formulation (Taylor & Figueroa, 2009) would be a suitable candidate for FSI simulation, although the computational cost would be exceedingly high, especially for a large arterial domain. Other FSI methods, such as the boundary element method–finite element method (BEM–FEM) (Ghalandari et al., 2019) and cut-cell immersed boundary method assisted by the adaptive mesh refinement algorithm (Salih et al., 2019) could also be useful tools for accurately depicting boundary interactions. The effects of a full FSI simulation on the overall results are still unclear, but Brown et al. (2012) found similar results in both the flow fields and helical flow indices of FSI and rigid wall models. Nevertheless, future work on patient-specific investigations of progressive carotid diseases, at least with a partial FSI model, would be important for accurate analysis of the wall shear stresses in patient-specific models (Sun et al., 2019; Toloui et al., 2012).

Second, despite employing five progressive CS cases for each patient model, only three patients had been analyzed. However, such an approach was reasonable since ACV simulations, especially in three dimensions, are computationally expensive in both time and effort (Coogan et al., 2013). Also, for a counterpart, one hundred and fifty CoW cases were generated to analyse the prevalence of the complete CoW, and the present study was the first study to investigate the effects of CS on cerebral vasculature with improved accuracy (Table 4, Figure 4B, 5A-1, 5A-2). Additionally, computational simulation minimized the unknown factors involved during the study, which might have been obstacles for accurate measurements in the clinical environment.

Third, the inflow conditions given for the patient-specific geometries were equivalent. The patient-specific aorta inflow conditions are usually not easy to obtain and were also unavailable for this study. Although a general mean inflow rate of 90 mL/s (Olufsen et al., 2000) was employed, the inflow rate in each patient would be different. In this circumstance, assigning arbitrarily different inflow conditions on patient cases is also another limitation of the study. The effects of patient-specific inflow rate conditions to patient-specific arterial domains and their differences to the results obtained with a general inflow rate are still unclear but future studies employing individual patient-specific inflow conditions would present a more refined patient-specific haemodynamic nature under CS progression.

Fourth, the use of the non-Newtonian fluid assumption would change the local haemodynamics. Although the conventional Newtonian fluid assumption holds for simulations of large arteries, such as the aorta and the cerebral artery (Arzani, 2018; Ku, 1997; Taylor & Figueroa, 2009), and is valid for the flows with shear rates higher than 100 s⁻¹ (Berger & Jou, 2000; Pedley & Luo, 1995), a recent comparative study showed a maximum difference of 17% in systolic velocity in a cerebral artery geometry with 90° bifurcation. Hence, a non-Newtonian assumption may induce notable haemodynamic effects in regions of significant geometrical variation, which could be an interesting topic for further investigation.

This study employed a three-dimensional ACV to simulate patient-specific haemodynamics during CS progression. Such an approach is computationally expensive,
as conventional modeling requires a repetitive modeling procedure for each patient-specific stenosis cases. Hence, a scheme to reduce the computational burden may include the adoption of reduced-order models (e.g., one-dimensional models) in artery segments of less importance. However, such an approach will neglect the accurate depiction of flow phenomena found in the three-dimensional system as the input to a three-dimensional domain from a one-dimensional domain cannot be equal to that from a three-dimensional domain. A network of one-dimensional and three-dimensional systems would consequently have discontinuities in the flow phenomena. A notable advance in the coherent blending of one and three-dimensional boundaries, effectively representing the entire three-dimensional domain may enable more realistic haemodynamic simulations at significantly reduced computational costs.

5. Conclusion

Predictive, progressive CS conditions were studied with ACV for the first time. As a result, transitional changes in the represented CoW were observed, where the prevalence of ‘complete’ CoW peaked at 50% CS and then declined. Such tendency, however, became statistically insignificant in groups of ‘< 70%’ and ‘> 70%’. The redirection of ipsilateral blood flow to other major arteries and the effective collateral capability of CoAs, activated from a degree of 75% and above, significantly contributed to this phenomenon, while hemispheric perfusion was preserved in the contralateral side and moderately sustained in the ipsilateral side. We discovered a new aspect of the conventional Windkessel model: it can demonstrate accurate flow reduction in the stenosed artery and bulk cerebral auto-regulation effects when a large arterial network, such as the aortic-cerebral domain, is used. In a manner similar to other literature reports, collateral flow through CoAs compensated for the reduced ipsilateral hemispheric perfusion but was activated only at severe CS. The presence of blood flow in CoAs at moderate CS may be due to an imbalance in hemispheric haemodynamic perfusion. This study should motivate more comprehensive predictive studies, which have been limited by statistical complexities and large engineering scales.

The use of a rigid wall, incompressible Newtonian assumptions, and a small number of patient samples are the primary limitations of this study. Future computational studies may need to adopt the specified limitations noted above for improved accuracy but would encounter extreme computational costs. Nonetheless, this study is a promising advancement in developing a mechanistic approach to the analysis of cardiovascular diseases.

Disclosure statement

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